

UynaMAT

DynaMAT Icelandic material

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Icelandic material

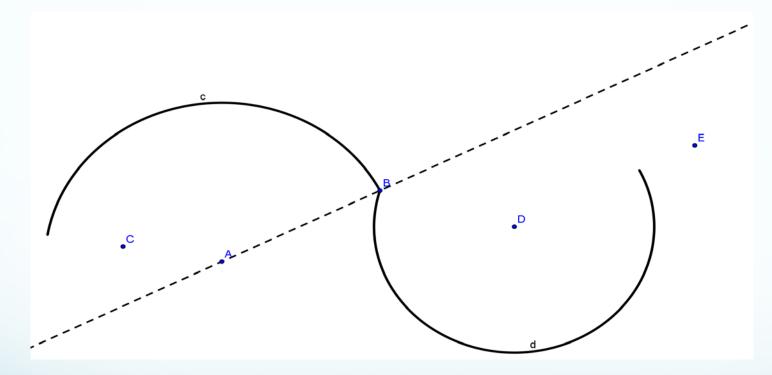
- Euclidean Eggs
- Using sliders to investigate functions, tangents and integrals
- Piecewise defined functions
- Investigating 2 by 2 matrices part I
- Investigating 2 by 2 matrices part II

Euclidean Eggs

- Experiment have fun
- Learn how to use some tools in GeoGebra
- Eggs

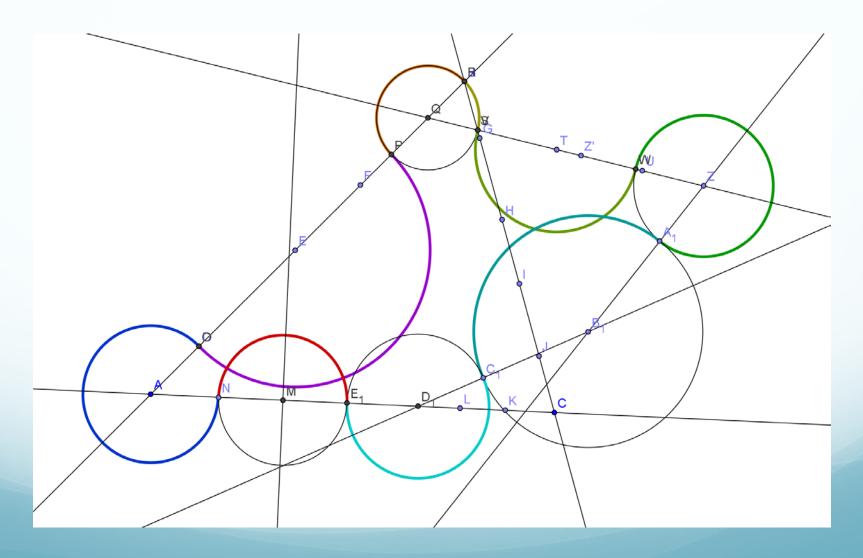


Principle

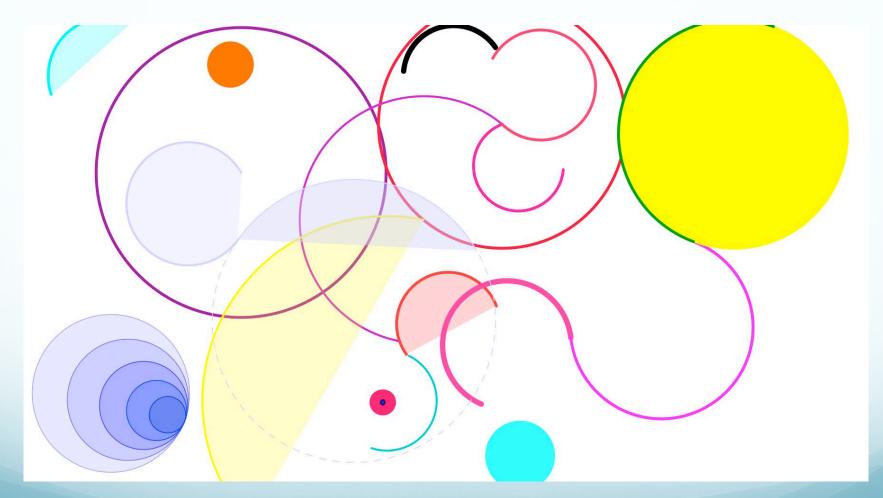


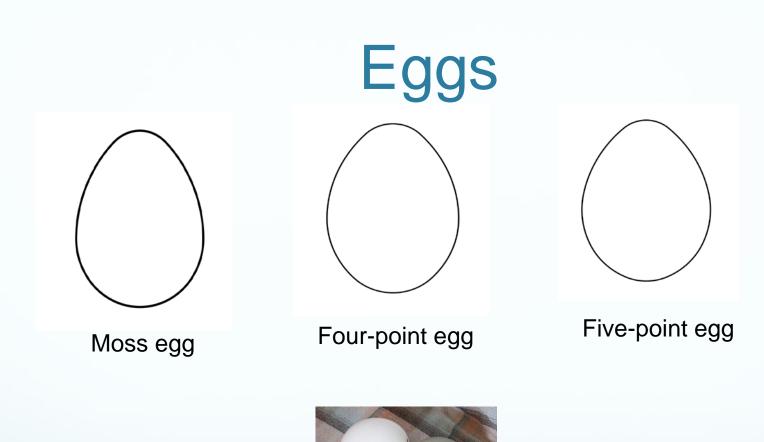
- When is the meeting of the arc smooth?
- two_arcs

Arcs and circles

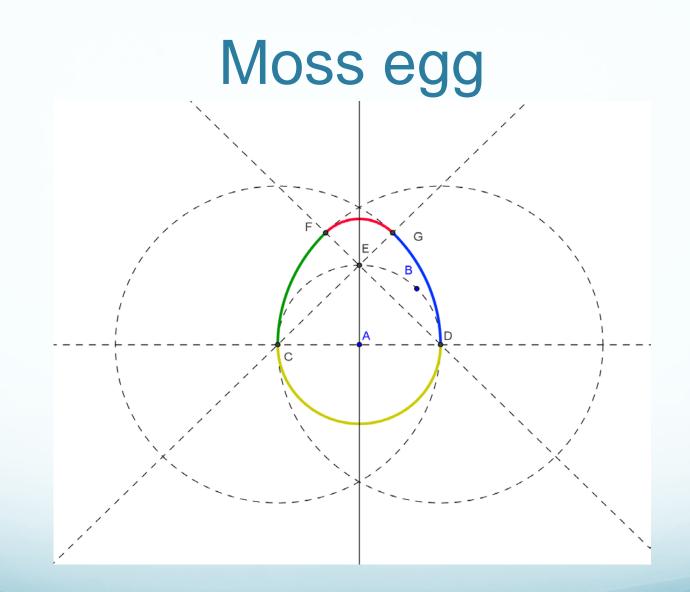


Arcs and circles



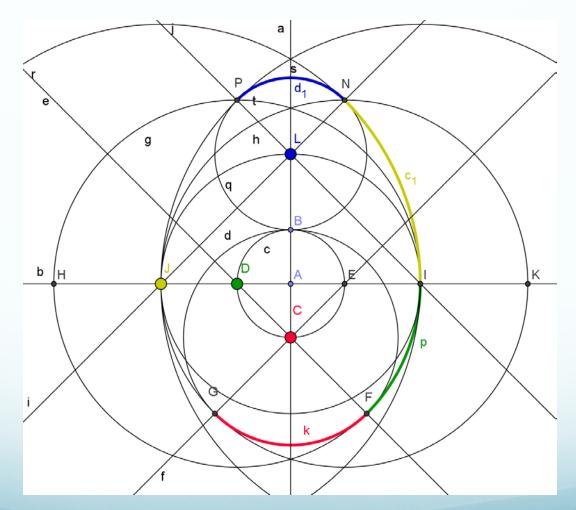


Source for Euclidean Eggs: Dixon, R. *Mathographics*. Basic Blackwell Limited, Oxford, England, 1987

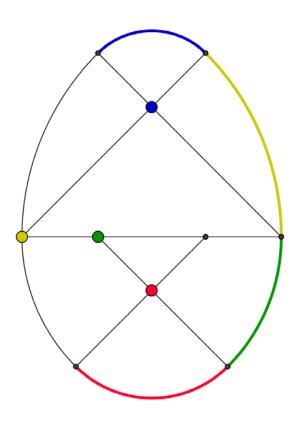


Moss egg, Variation of a Moss egg

Four-point egg



Four-point egg



GeoGebra files

- Four-point egg
- Five-point egg
- Experiment_circles
- <u>Spiral</u>

Chapters on linear algebra – Two graphic views

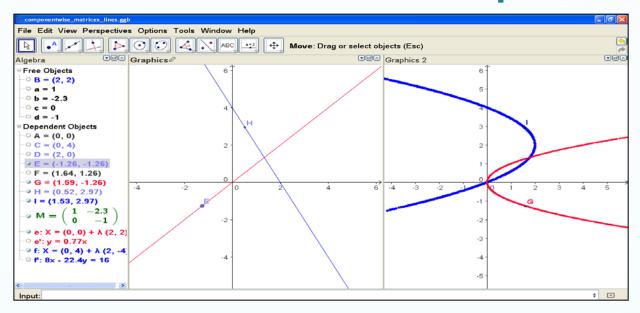
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Image of the unit square

Two graphic views

- In GeoGebra 4.0 the option of having two graphic views open at the same time makes it possible to study maps from the plane to plane
- Linear maps are particularly easy to study
- There are two ways to do this:
 - defining a 2 x 2 matrix <u>unit_square</u>, <u>determinant</u>
 - defining the action on one point and using the trace option – this can also be used for nonlinear maps and complex maps

Nonlinear map



The method above can be used for *any* transformation, even non-linear ones. Say we want to study the map $(x, y) \rightarrow (x \cdot y, y)$

We define a point E on a line and then the point G = (x(E) * y(E), y(E))in Graphic view 2. We then put the trace on G and move the point E along the line and watch the <u>image trace out a curve in Graphics 2</u>.

Maps from the complex numbers to the complex numbers

• We can use a similar method to study maps from C to C, e.g. $z \rightarrow \frac{z+2}{z-1}$

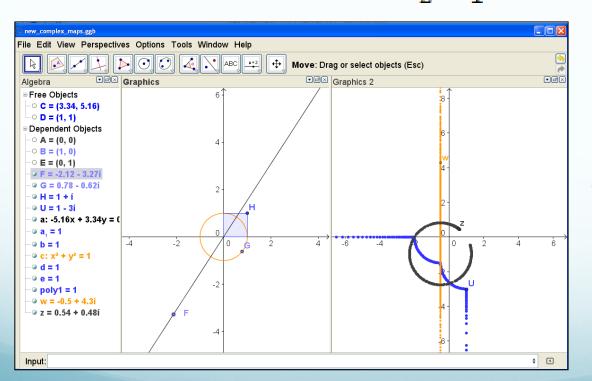


Image of a line, circle and the boundary of a square